# Synthesis and Crystal Structure of $\boldsymbol{\beta}-\mathbf{S r V}_{\mathbf{2}} \mathbf{O}_{\mathbf{6}}$ 

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#### Abstract

The preparation and growth of single crystals together with a crystal structure determination of $\beta-\mathrm{SrV}_{2} \mathrm{O}_{6}$ are reported. This high temperature form of $\mathrm{SrV}_{2} \mathrm{O}_{6}$ crystallizes in the orthorhombic system, space group Pnma, with $a=9.666$ (1) $\AA, b=3.6808$ (4) $\AA, c=12.529$ (3) $\AA, Z=4$. The structure, determined and refined down to $R=3.1 \%$, is described as isolated zigzag double strings with $\left[\mathrm{V}_{2} \mathrm{O}_{6}\right]_{n}$ composition extending along the [010] direction and built up by edge-sharing $\mathrm{VO}_{6}$ octahedra. Strontium atoms occupy tricapped trigonal prisms of oxygen atoms pertaining to three different strings and assume the stability of the network. © 1991 Academic Press, Inc.


## Introduction

Several phases pertaining to the $M O$ $\mathrm{V}_{2} \mathrm{O}_{5}-\mathrm{VO}_{2}$ systems ( $M=\mathrm{Ca}, \mathrm{Sr}, \mathrm{Ba}$ ) had been investigated (1-7). In the perspective of an investigation of vanadates with lower vanadium oxidation number (III or IV) obtained by reduction of vanadates containing vanadium V , it was advisable to deepen some of their structural data. The polymorphism in $\mathrm{Sr}_{2} \mathrm{~V}_{2} \mathrm{O}_{7}$ had already been indicated (3); single crystals corresponding to a new polymorphic form have been obtained and their study is in progress. Presently, the polymorphism of $\mathrm{Sr}_{2} \mathrm{O}_{6}$ has also been established, and the aim of this paper is to report about the synthesis and the structure of the high temperature form, $\beta-\mathrm{SrV}_{2} \mathrm{O}_{6}$.

## Experimental

Strontium carbonate and vanadium pentoxide with molar ratio $1: 1$ were intimately
mixed, prefired at $670^{\circ} \mathrm{C}$ during 24 hr under an oxygen stream to remove carbon dioxide, reground, and heated again for 24 hr at the same temperature. The obtained yellow product exhibits the X-ray powder pattern already reported by Bouloux and Galy (8) and indexed in the orthorhombic system, space groups $C 222, C m m 2$, or $C m m m$, with the parameters $a=8.245 \AA, b=12.293 \AA$, and $c=7.657 \AA$. In order to obtain crystals, a melting of the powder was performed at $830^{\circ} \mathrm{C}$, followed by a cooling down to $530^{\circ} \mathrm{C}$ at the rate of $5^{\circ} \mathrm{C} / \mathrm{hr}$, then down to room temperature at $60^{\circ} \mathrm{C} / \mathrm{hr}$. Pale yellow parallelepipedic single crystals were isolated from the material. The corresponding powder pattern was different from the previous one; a new polymorphic form of $\mathrm{SrV}_{2} \mathrm{O}_{6}$ was probably obtained. A selected crystal was studied using a precession camera with molybdenum $K \alpha$ radiation.

The compound crystallizes in the orthorhombic system; the possible space groups are Pnma or $P_{n 2}{ }_{1} a$. The full collection of

TABLE I
Physical and Crystallographic Data

| Formula | $\mathrm{Sr}^{2} \mathrm{O}_{6}$ |
| :---: | :---: |
| Molecular weight (g) | 285.5 |
| Color | pale yellow |
| Morphology | parallelepiped |
| Dimension (mm) | $0.12 \times 0.12 \times 0.17$ |
| Crystal system | orthorhombic |
| Space group | Pnma ( ${ }^{0} 62$ ) |
| $a(\AA)$ | 9.666 (1) |
| $b(\AA)$ | 3.6808(4) |
| $c(\AA)$ | 12.529(3) |
| $V\left(\AA^{3}\right)$ | 445.7(1) |
| $Z$ | 4 |
| $\rho$ calc ( $\mathrm{g} \mathrm{cm}^{-3}$ ) | 4.26 |
| $F(000)$ | 528 |
| $\mu(\mathrm{MoKa})\left(\mathrm{cm}^{-1}\right)$ | 156 |
| Wavelength (MoKa) ( $\AA$ ) | 0.71069 |
| Munocluromator | oriented graphite |
| Take off ( ${ }^{\circ}$ ) | 3.75 |
| Detector width ( $\mathrm{mm}^{2}$ ) | $4 \times 4$ |
| Scan type | $\omega / 2 \theta$ |
| Scan width ( ${ }^{\circ}$ ) | $0.75+0.35 \tan \theta$ |
| Prescan speed ( ${ }^{\circ} \mathrm{mn}{ }^{-1}$ ) | 10 |
| Maximum time (sec) | 80 |
| Reflections for cell refinement | 25 |
| Recorded reflections | 1025, $2 \theta \leq 70^{\circ}$ |
| $h k l$ range | $\begin{aligned} & 0 \leq h \leq 15,0 \leq k \leq 5,0 \leq l \leq \\ & 20 \end{aligned}$ |
| Intensity control reflections | $008 / 0-40 / 800$ every 3600 sec |
| Orientation control reflections | 10-13/605 every 250 refl. |
| Transmission coefficient range | 0.41-1.00 |
| Number of unique data with $I \geq 3 \sigma$ | 705 |
| Number of refined parameters | 56 |
| $R$ | 0.031 |
| $R_{w}(\boldsymbol{w}=1)$ | 0.037 |

data had been performed on a CAD4 Enraf-Nonius diffractometer; the refined cell parameters are $a=9.666(1) \AA, b=$ $3.6808(4) \AA$, and $c=12.529(3) \AA$ and allow one to index all the lines of the powder pattern. The studied compound is a new high temperature form of $\mathrm{SrV}_{2} \mathrm{O}_{6}$, called $\beta$ $\mathrm{Sr}_{2} \mathrm{O}_{6}$.

## Structure Determination

All the experimental X-ray data and results are summarized in Table I. Corrections of X-ray flux fluctuations, Lorentz polarization, and absorption (9) had been applied to the $h k l$ data. The structure was determined using the Patterson method and its refinement was carried out via full matrix least-
squares calculations in the space group Pnma. This space group was chosen because, first, an inspection of $h 0 l$ and $h 2 l$ intensities revealed that their distributions are virtually identical, suggesting that all atoms were situated on, or very near, the levels $y= \pm 1 / 4 b$ (classical case for these structures with a parameter near $3.6 \AA$ ); second, statistics tests are in favor of the centrosymmetric group, and a refinement carried out with the $P n 2_{1} a$ space group has given very strong correlations between parameters ( 35 coefficients higher than 0.999 ). Atomic scattering factors were corrected for anomalous dispersion (10). Secondary extinction had been applied ( $r^{*}=5,43$ ) (11). The calculations and drawings were performed with CRYSTALS (12) and ORTEP (13) using a superminicomputer VFX/80 ALLIANT. The structural details of $\beta$ $\mathrm{SrV}_{2} \mathrm{O}_{6}$ are summarized in Tables II and III.

TABLE II
Fractional Coordinates and Thermal Parameters

| Atom | $x$ | $y$ | $z$ | $B_{\text {eq }}\left(\AA^{2}\right)$ |
| :---: | :---: | :---: | :---: | :---: |
| Sr | 0.63235 (7) | 1/4 | $0.38073(5)$ | 0.52(4) |
| V1 | 0.0018(1) | 1/4 | 0.6255 (1) | 0.30(6) |
| V2 | 0.2441(1) | 1/4 | $0.41085(9)$ | 0.28(6) |
| O1 | $0.1733(5)$ | 1/4 | $0.6081(4)$ | 0.4(2) |
| 02 | -0.0294(6) | 1/4 | 0.7545(4) | $0.7(3)$ |
| 03 | -0.1966(5) | 1/4 | 0.5647 (4) | 0.5(2) |
| 04 | $0.0339(5)$ | 1/4 | 0.4120(5) | $0.5(2)$ |
| O5 | $0.2837(6)$ | 1/4 | $0.2858(4)$ | 0.7(2) |
| 06 | $0.3964(5)$ | 1/4 | 0.4788(4) | $0.6(2)$ |
| Atom | $\beta_{11}$ | $\beta_{22}$ | $\beta_{33}$ | $\beta_{13}$ |
| Sr | 0.00173 (7) | $0.0087(4)$ | $0.00075(4)$ | 0.00016(3) |
| V1 | $0.00044(9)$ | 0.0069(6) | $0.00081(5)$ | -0.00020(7) |
| V2 | 0.00051 (9) | n.0067(6) | 0.00053 (5) | 0.00002 (7) |
| 01 | $0.0006(4)$ | $0.015(3)$ | 0.0010(3) | -0.0002(3) |
| 02 | 0.0019 (7) | 0.015 (3) | 0.0010(3) | -0.0003(3) |
| 03 | $0.0011(4)$ | $0.006(3)$ | $0.0011(3)$ | $0.0002(3)$ |
| 04 | $0.0006(4)$ | 0.011(3) | 0.0018(3) | -0.0003(3) |
| O5 | $0.0027(4)$ | 0.016 (3) | $0.0006(3)$ | -0.0003(3) |
| O6 | $0.0008(4)$ | 0.010(3) | 0.0013(3) | $0.0000(3)$ |

Note. All atoms are situated in site $4 c$ (Wyckoff notation). $B_{\mathrm{eq}}=4 / 3 \Sigma_{i j}\left(a_{i} a_{j}\right) \beta_{i j}$. The form of anisotropic displacement parameter is $\exp \left[-\left(\beta_{11} h^{2}+\beta_{22} k^{2}+\beta_{33}{ }^{2}+2 \beta_{12} h k+2 \beta_{13}\right.\right.$ $\left.\left.h l+2 \beta_{23} k l\right)\right] . \beta_{12}$ and $\beta_{23}$ are fixed to 0 .

TABLE III
Selected Interatomic Distances ( $\AA$ ) and O-V-O Angles ( ${ }^{\circ}$ )

|  | $\mathrm{Sr}-\mathrm{Ol}_{\text {iili/iv }}$ | 2.634(3) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{Sr}-\mathrm{O} 2_{\text {vivi }}$ | 2.623(4) |  |  |  |  |
|  | $\mathrm{Sr}-\mathrm{O} 3_{\text {vii }}$ | 2.837(5) |  | V1-V2 | 3.566(2) |  |
|  | $\mathrm{Sr}-\mathrm{OS}_{\text {vii }}$ | 2.548(5) |  | $\mathrm{V} 1-\mathrm{V} 2_{\text {ii }}$ | 3.040(1) |  |
|  | Sr -06 | $2.591(5)$ |  |  |  |  |
|  | $\mathrm{St}-06{ }_{\text {iilijv }}$ | $2.561(4)$ |  |  |  |  |
| V1 | 01 | 02 | 03 | O4 | $\mathrm{O}_{\mathrm{i}}$ | $\mathrm{O}_{4 i}$ |
| 01 | 1.672(5) | 108.1(3) | 150.8(3) | 75.9(2) | 98.4(2) | 98.4(2) |
| 02 | 2.684(8) | $1.644(6)$ | 101.1(2) | 176.1(2) | 101.9(2) | 101.9(2) |
| 03 |  | $2.876(8)$ | $2.063(5)$ | 75.0(2) | 75.2(2) | 75.2(2) |
| 04 | 2.802(8) |  | $2.937(7)$ | 2.693 (6) | $77.2(2)$ | 77.2(2) |
| O4, | 2.732(5) | 2.782(6) | $2.438(5)$ | 2.946 (9) | $1.930(2)$ | 144.9(3) |
| O4ii | 2.732(5) | $2.782(6)$ | 2.438 (5) | 2.946(9) |  | 1.930(2) |
| V2 | 01 | $03_{i}$ | $\mathrm{O3}_{\text {ii }}$ | 04 | 05 | 06 |
| 01 | 2.564(5) | 77.4(2) | 77.4(2) | 74.1(2) | 178.3(2) | 75.4(2) |
| $\mathrm{O3}_{1}$ | 2.850(6) | 1.921(1) | 146.6(3) | 76.1(2) | $102.2(2)$ | 97.3(2) |
| $\mathrm{O3}_{\text {ii }}$ | 2.850(6) |  | 1.921(1) | 76.1(2) | $102.2(2)$ | 97.3(2) |
| 04 | 2.802(8) | $2.438(5)$ | $2.438(5)$ | 2.032 (5) | 104.1(3) | 149.5(3) |
| 05 |  | $2.758(6)$ | 2.758(6) | $2.886(8)$ | 1.613(6) | 106.3(3) |
| 06 | 2.697(7) | $2.723(5)$ | 2.723(5) |  | 2.653(7) | 1.701(5) |

Note. (i) $-x,-y, 1-z$; (ii) $-x, 1-y, 1-z$; (iii) $1-x$, $1-y, 1-z$; (iv) $1-x,-y, 1-z$; (v) $1 / 2-x, 1 / 2+y$, $-1 / 2+z$; (vi) $1 / 2-x,-1 / 2+y,-1 / 2+z$; (vii) $1 / 2+x, y$, $1 / 2-z$; (viii) $1+x, y, z$.

## The Structure of $\boldsymbol{\beta}-\mathrm{Sr}_{\mathbf{2}} \mathrm{O}_{6}$

The projection of the structure onto the (010) plane is given in Fig. 1. The two independent vanadium atoms (V1 and V2) are octahedrally surrounded by oxygen atoms. Two octahedra having an edge in common, by additional edge-sharing to similar pairs, above and below, lead to zigzag double strings extending along the $b$-axis (Fig. 2). All the atoms lie in the mirror planes of the space group Pnma (position 4c). These isolated strings with $\left[\mathrm{V}_{2} \mathrm{O}_{6}\right]_{n}$ composition are packed with the same orientation in layers parallel to the ( 001 ) plane, with orthogonal directions (nearly [101] and [10 $\overline{1}]$ ) in every other layer, making an infinite puckered network. Strontium atoms occupy tricapped trigonal prisms of oxygen atoms pertaining to three different strings and cement the structure.

Further study of the vanadium coordination polyhedra (Fig. 2 and Table III) shows,


Fig. 1. Projection of $\beta-\mathrm{Sr}_{2} \mathrm{O}_{6}$ onto the plane ( 010 ), large circles are strontium atoms, intermediate ones are oxygen atoms, and the small ones are vanadium. Atoms in heavier outline are at $y=3 / 4$, the lighter ones at $y=1 / 4$.
as in previously described structures, $V$ atoms are moved toward one of the apexes of the octahedron, i.e., O2 for V1 and O5 for V2, giving the shortest distances (double bond character $\mathrm{V}=\mathrm{O}$ ), respectively $\mathrm{V} 1-\mathrm{O} 2$ and V2-O5, symmetrically opposed to the longest ones, V1-O4 and V2-O1. The found distances are in agreement with the ones already encountered and discussed, for example, in the recently refined $\mathrm{V}_{2} \mathrm{O}_{5}$ structure (14) and metavanadates $\mathrm{CaV}_{2} \mathrm{O}_{6}(15,16)$ $\alpha$ - and $\beta-\mathrm{CdV}_{2} \mathrm{O}_{6}(16,17), \alpha$ - and $\beta-\mathrm{CuV}_{2} \mathrm{O}_{6}$ (18-20). This tendency of vanadium V for square pyramidal coordination (SP) (V1 and V2 being respectively at 0.44 and $0.45 \AA$ from the basal plane of the SP (O1O3O4 $\mathrm{O}_{\mathrm{ii}}$ and $\left.\mathrm{O}_{\mathrm{i}} \mathrm{O}_{\mathrm{ii}} \mathrm{O} 4 \mathrm{O} 6\right)$ ) induces a rather large V1-V2 distance across the shared edge in the plane (010), (i.e. $3.566(2) \AA$ ) while the $\mathrm{V} 1-\mathrm{V} 2_{\mathrm{ii}}$ distance shrinks to 3.040(1) $\AA$. The second short $\mathrm{V}-\mathrm{O}$ distances


FIG. 2. Perspective view of a $\left[\mathrm{V}_{2} \mathrm{O}_{6}\right]_{n}$ string extending along the $b$-axis.
are V1-O1 and V2-O6; they correspond to unshared oxygen atoms which are on the border of the strings and interact mainly with strontium atoms. The strings exhibit in their internal association a weakness in the bonding, V-O distances being respectively at 2.693(6) $\AA$ and $2.564(5) \AA$.

The environment of strontium $(\mathrm{CN}=9)$ is a tricapped trigonal prism (Fig. 3). Eight $\mathrm{Sr}-\mathrm{O}$ distances range from $2.548(5)$ to $2.634(3) \AA$; the last one, $\mathrm{Sr}-\mathrm{O} 3_{\text {viii }}$, through a rectangular face of the trigonal prism, slightly longer ( $2.837(5) \AA$ ), corresponds to an oxygen firmly linked to two vanadium atoms. Dihedral angles between the faces of the trigonal prism are $47.0,65.2$, and $67.8^{\circ}$.

## Discussion

The structure of $\beta-\mathrm{SrV}_{2} \mathrm{O}_{6}$ appears to be isostructural with $\mathrm{PbV}_{2} \mathrm{O}_{6}$ studied by Jordan and Calvo (21) and hence rather different from the one found for $\mathrm{CaV}_{2} \mathrm{O}_{6}, \alpha$ - and $\beta$ $\mathrm{CdV}_{2} \mathrm{O}_{6}, \alpha$ - and $\beta-\mathrm{CuV}_{2} \mathrm{O}_{6}(15-20)$, and the brannerite $\mathrm{ThTi}_{2} \mathrm{O}_{6}$ (22). Nevertheless dou-
ble strings $\left[M_{2} \mathrm{O}_{6}\right]$ have already been reported by Wadsley in the alkalinotitaniobates $\mathrm{KTiNbO}_{5}, \mathrm{KTi}_{3} \mathrm{NbO}_{9}$ (23), and by Lavaud and Galy in $\mathrm{Cu}_{x} \mathrm{~V}_{4} \mathrm{O}_{11}$ (24), but in these cases they are linked to each other by


Fig. 3. Coordination polyhedron of the strontium atom.


FIG. 4. Projection of the idealized structure of $\beta-\mathrm{Sr}_{2} \mathrm{O}_{6}$ (a), " $\mathrm{SrV}_{2} \mathrm{O}_{5}$ " (b), " $A \mathrm{~B}_{2} \mathrm{O}_{6}$ " (c), and $\mathrm{KTiNbO}_{5}$ (d).
corner-sharing in order to accommodate the various stoichiometries.
Looking at the idealized structure of $\beta-\mathrm{SrV}_{2} \mathrm{O}_{6}$ and $\mathrm{KTiNbO}_{5}$ (Fig. 4a and 4d), their similarities prompt one to imagine that the former can give by reduction a possible " $\mathrm{Sr}_{2} \mathrm{O}_{5}$ " layer structure (Fig. 4b). This structural transformation is achieved via a crystallographic shear operation with a $1 / 2$ [100] slip of every other layer parallel to the (001) plane. Finally, it leads to the assembly of $\left[\mathrm{V}_{2} \mathrm{O}_{6}\right]_{n}$ strings by corner-sharing, giving puckered $\left[\mathrm{V}_{2} \mathrm{O}_{5}\right]_{n}$ layers parallel to the (100) plane. During this operation strontium atoms are moved in order to hold together the layers. The latter, $\mathrm{KTiNbO}_{5}$, could lead, by an inverse process to an $\mathrm{AB}_{2} \mathrm{O}_{6}$ network (Fig. $4 c$ ) very similar to $\beta-\mathrm{SrV}_{2} \mathrm{O}_{6}$.
The phase transition $\alpha \rightarrow \beta$, which occurs in $\mathrm{SrV}_{2} \mathrm{O}_{6}$ around $675^{\circ} \mathrm{C}$, is accompanied by a drastic decrease of the packing efficiency,
$V_{\alpha}=129.3 \AA^{3}$ against $V_{\beta}=111.5 \AA^{3}$ per unit. The study of this transition and the crystal structure of $\alpha-\mathrm{SrV}_{2} \mathrm{O}_{6}$ will be discussed in a forthcoming paper.

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## References

1. R. Kohlmuller and J. Perraud, Bull. Soc. Chim. Fr. 5, 642 (1964).
2. J. C. Bouloux and J. Galy, Acta Crystallogr., Sect. B: Struct. Crystallogr. Cryst. Chem. B29, 269 (1973).
3. J. C. Bouloux, J. Galy, and P. Hagenmuller, Rev. Chim. Miner. 11, 48 (1974).
4. J. C. Bouloux and J. Galy, J. Solid State Chem. 16, 385 (1976).
5. M. Cyrot, B. Lambert-Andron, J. L. Soubeyroux, M. J. Rey, Ph. Dehauht, F. Cyrot-Lack-
mann, G. Fourcaudot, J. Beille, and J. L. Tholence, J. Solid State Chem. 85, 321 (1990).
6. M. J. Rey, Ph. Dehauht, J. C. Joubert, B. Lam-bert-Andron, M. Cyrot, and F. Cyrot-Lackmann, J. Solid State Chem. 86, 101 (1990).
7. M. Itoh, M. Shikano, R. Liang, H. Kawai, and T. Nakamura, J. Solid State Chem. 88, 597 (1990).
8. " $\mathrm{SrV}_{2} \mathrm{O}_{6}$, No 27-1444, Joint Committee on Powder Diffraction Standards, Swarthmore, PA."
9. N. Walker and D. Stuart, Acta Crystallogr., Sect. A: Found. Crystallogr. A39, 158 (1983).
10. D. T. Cromer and J. T. Waber, "International Tables for X-ray Crystallography," Vol. IV, Kynoch Press, Birmingham, UK (1974).
11. A. C. Larson, Crystallogr. Comput. Tech., 291 (1969).
12. D. J. Watkins, J. R. Carruthers, and P. W. Betterige, "Crystals, Users Guide," Chem. Crystal. Laboratory Univ., Oxford, UK, (1985).
13. C. K. Johnson, "Ortep II Report ORNL 5138," Oak Ridge National Laboratory, Oak Ridge, TN, (1976).
14. R. Enjalbert and J. Galy, Acta Crystallogr., Sect C: Cryst. Struct. Commun. C42, 1467, (1986).
15. G. Perez, J. C. Bouloux, B. Frit, and J. Galy, C.R. Acad. Sci. Paris Sér. C 270, 952 (1970).
16. J. C. Bouloux, G. Perez, and J. Galy, Bull. Soc. Fr. Mineral. Cristallogr. 95, 130 (1972).
17. J. C. Bouloux and J. Galy, Bull. Soc. Chim. Fr. 130, 736, (1969).
18. D. Lavaud and J. Galy, Bull. Soc. Fr. Mineral. Cristallogr. 95, 134 (1972).
19. R. Calvo and D. Manolescu, Acta Crystallogr., Sect B: Struct. Crystallogr. Cryst. Chem. B29, 1743, (1973).
20. D. Mercurio, J. Galy, and B. Frit, C.R. Acad. Sci. Paris Sér. C 282, 27 (1976).
21. B. D. Jordan and C. Calvo, Can. J. Chem. 52, 2701 (1974).
22. R. Ruh and A. D. Wadsley, Acta Crystallogr. 21, 974 (1966).
23. A. D. Wadsley, Acta Crystallogr. 17, 623 (1964).
24. J. Galy and D. Lavaud, Acta Crystallogr., Sect. B: Struct. Crystallogr. Cryst. Chem. B27, 1005 (1971).
